



The disc embedding theorem

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Instructional and educational works.

Monografía

This text contains the first thorough and approachable exposition of Freedman's proof of the disc embedding theorem

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Título: The disc embedding theorem editors, Stefan Behrens [et al.]

Edición: First edition

Editorial: Oxford, UK Oxford University Press [2021] 2021

Descripción física: 1 online resource (xvii, 473 pages) illustrations (black and white, and colour)

Mención de serie: Oxford scholarship online

Nota general: This edition also issued in print: 2021

Bibliografía: Includes bibliographical references and index

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Audiencia: Specialized

ISBN: 0-19-187692-5 0-19-257838-3

Materia: Differential topology Mathematics- Study and teaching

Autores: Behrens, Stefan, author

Enlace a formato fisico adicional: 0-19-884131-0

Punto acceso adicional serie-Título: Oxford scholarship online

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